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Incentives in Hedge Funds

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Hedge Fund as Delegated Portfolio Management

Investor (Unsophisticated) 1 Unit of Fund, No Withdrawal

Manager M Units of Personal Fund: Manage Investor's and Personal Funds

'Separate Management' or 'Equity Stake'

Weak Regulation, Low Transparency

Generate Alpha

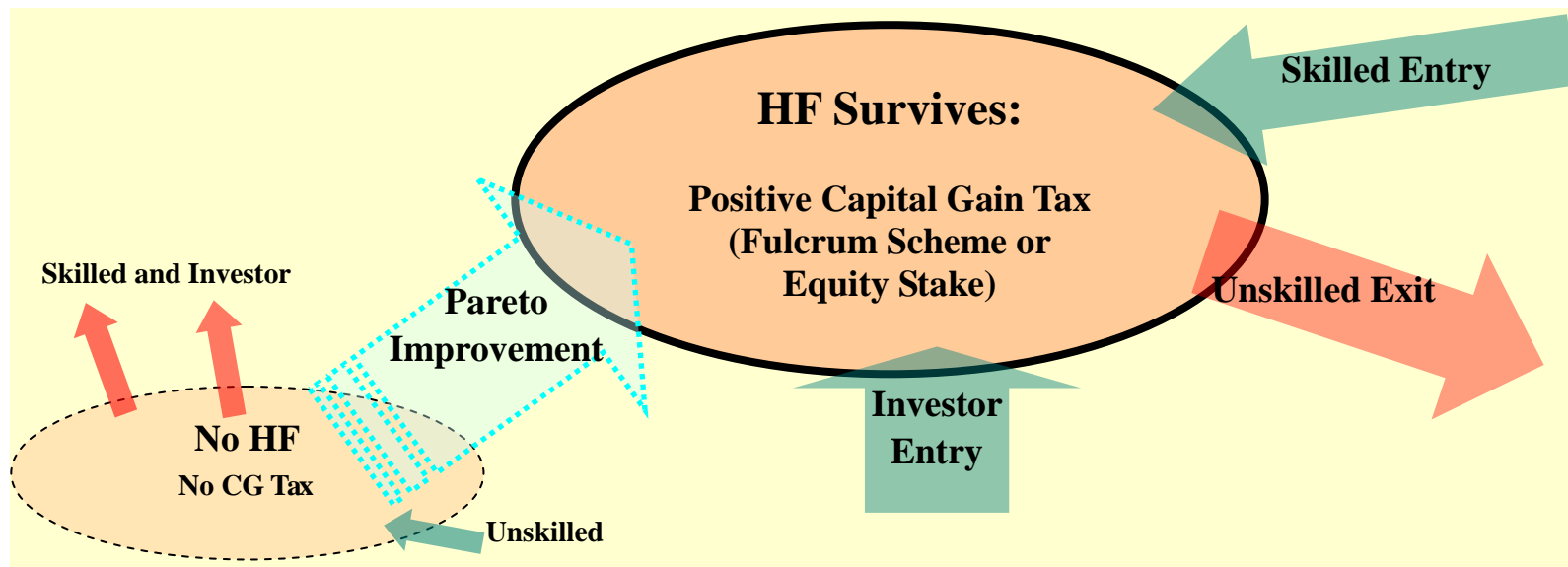
Manager	{	Skilled Type	Select Alpha (Action) $a \in [0, \infty)$ with Non-Pecuniary Cost $C(a)$
		Unskilled Type	Alpha 0

Incentive Problem

Hidden Type
Hidden Activity

Investor Cannot Identify whether Manager is skilled or not
Investor Cannot Observe Manager's Activity

Q: Can We Solve Incentive Problem?

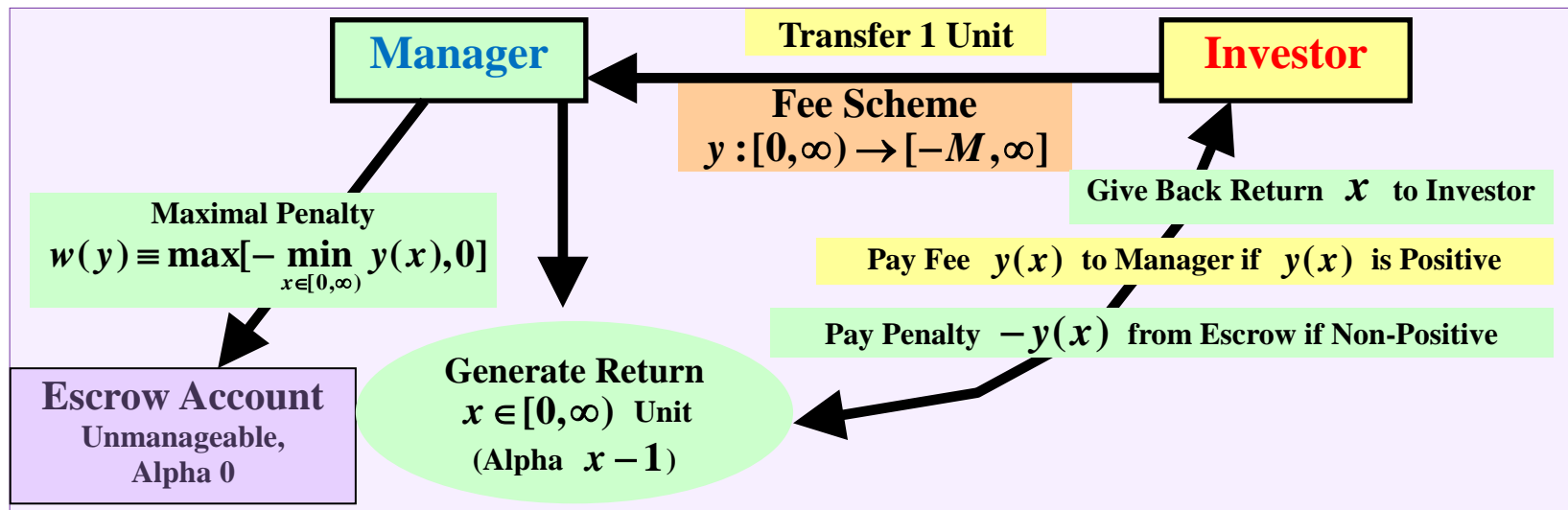


A: Yes, but We Need Capital Gain Tax!

Manager's Incentive Fee Scheme

$$y : [0, \infty) \rightarrow [-M, \infty), \quad y(x) \in [-M, \infty)$$

Return-Contingency, Penalty, Escrow for Solvency



Real Fee Scheme

‘2:20’ Scheme

Asymmetry, No Penalty, Convexity, High-Powered

$$y(x) = 0.2x + 0.02$$

Criticisms (Warren Buffet): ‘2:20’ Makes Manager More Risk-Taking by Side Contracting with Third Party. We Should Change ‘2:20’ Scheme to

‘Fulcrum’ Scheme

Symmetric, Positive Penalty, Linear, Low-Powered

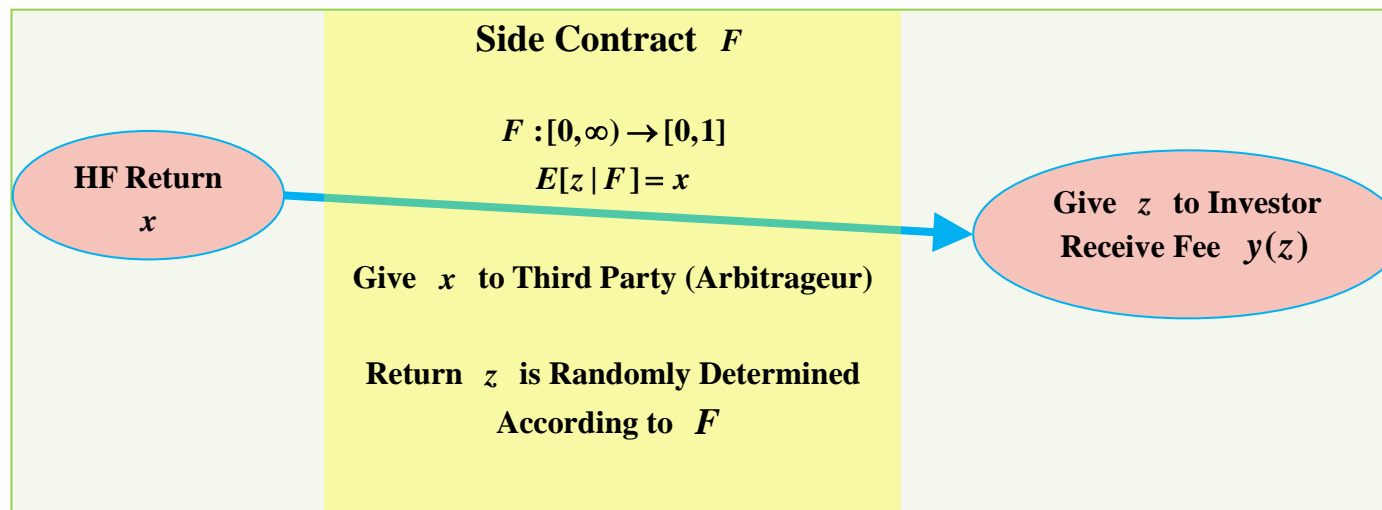
$$y(x) = k(x - 1)$$

Side Contracting: Performance Mimicry

Randomize Return

Cumulative Distribution $F : [0, \infty) \rightarrow [0, 1]$

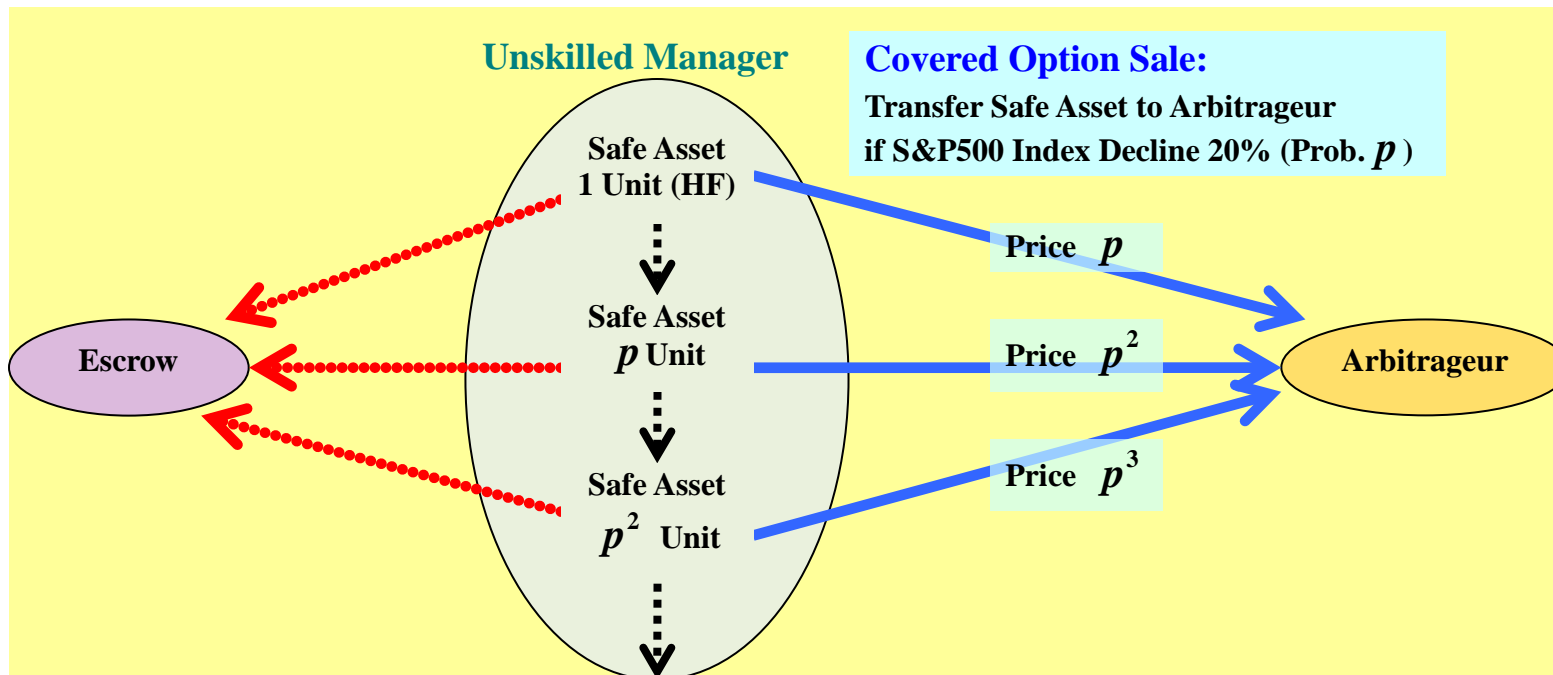
$$E[z | F] = x$$



Example (Lo (2001))

Capital Decimation Partners (CDP)

Unskilled Can Generate Alpha $\frac{p}{1-p} > 0$ with Prob. $1-p$



Previous Works: Hedge Fund Never Survives

Foster + Young (08/09)

With No CG Tax, No Scheme Can Solve Incentive Problem

Media:

FT (18/3/08), NYT (3/8/08)

“HF Never Survives. We Need More Transparency!”

Results of This Paper

▪ **CG Tax Functions**

- **With No CG Tax, We Cannot Solve Incentive Problem (a la Foster + Young)**
- **With Positive CGT Rate $t > 0$, We Can Solve Incentive Problem**

▪ **Constrained Optimal Scheme**

- **Fulcrum After Taxation: Low-Powered**

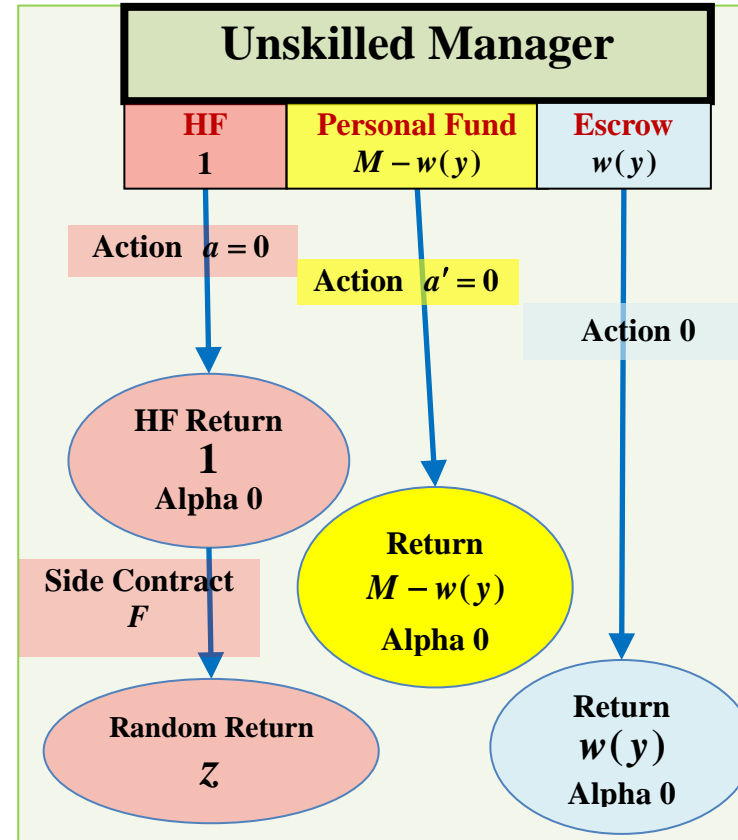
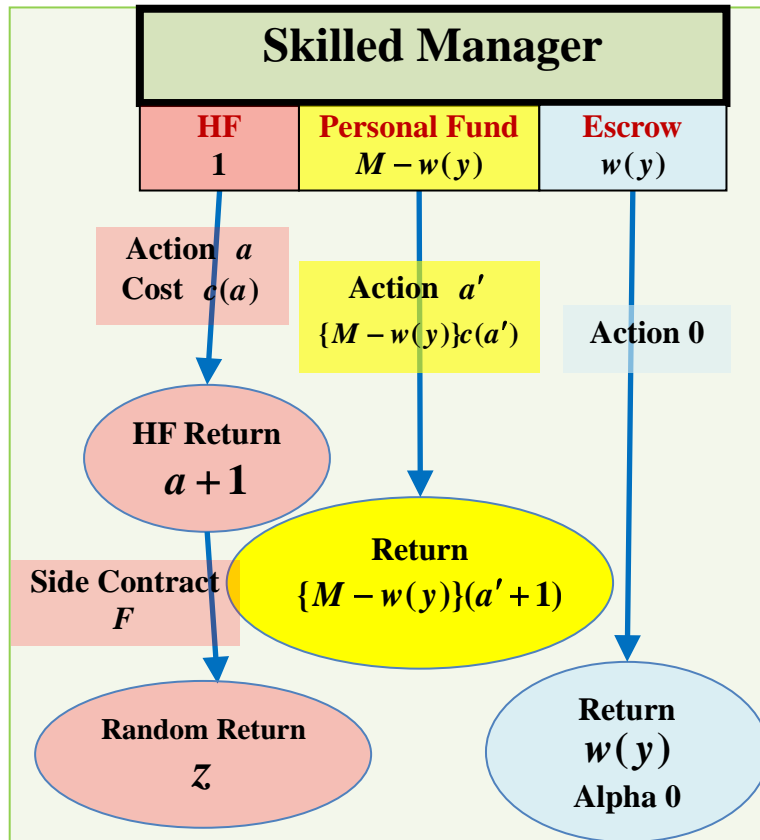
▪ **Income Tax on Fee Functions**

- **Income Tax Rate Should be Greater than CG Tax Rate, $\tau > t$**
- **Manager Selects Constrained Optimal Scheme Voluntarily**

▪ **Equity Stake Functions**

- **We Can Solve Incentive Problem without Fulcrum**

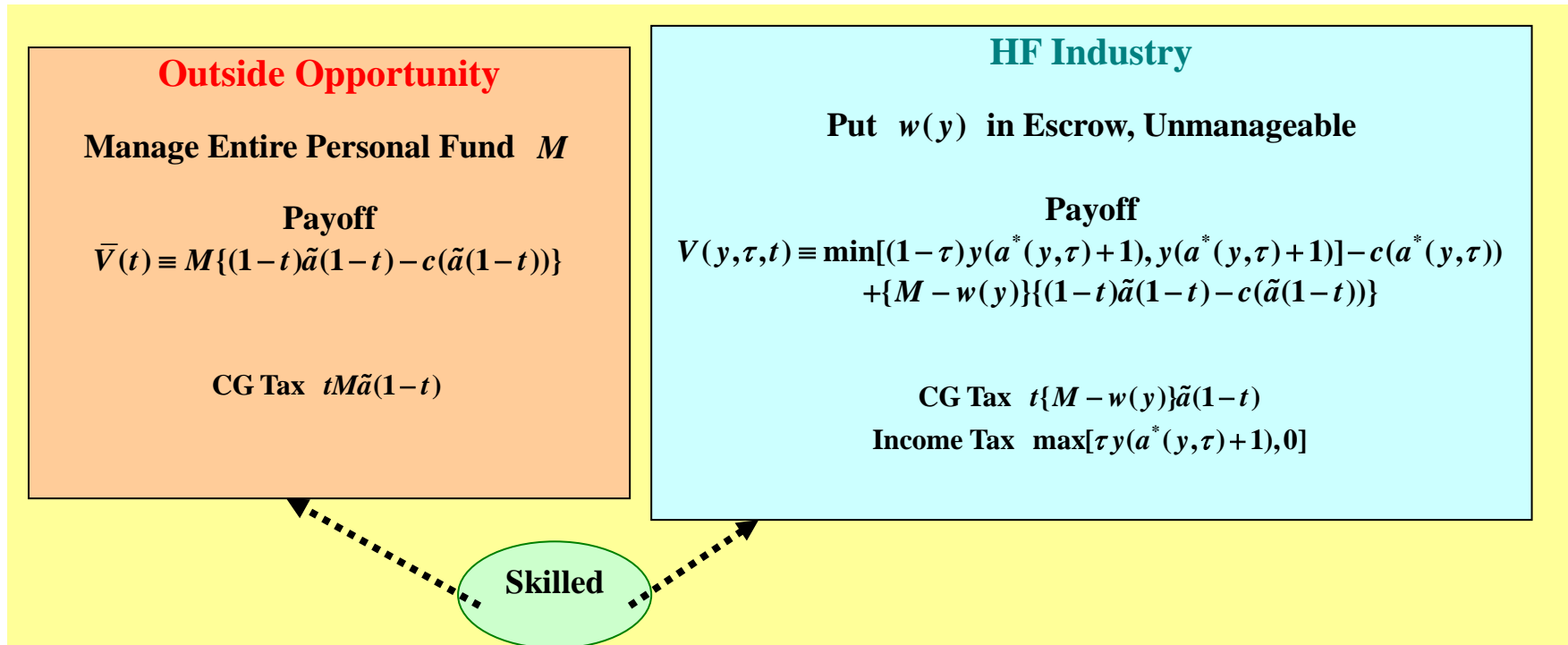
Assumption: Separate Management



Incentive Problem: Five Constraints

- ① **Skilled Entry**
- ② **Unskilled Exit**
- ③ **Investor Entry**
- ④ **Welfare Improvement**
- ⑤ **Skilled Non-mimicry: Skilled Needs No Third-Party Side Contract**

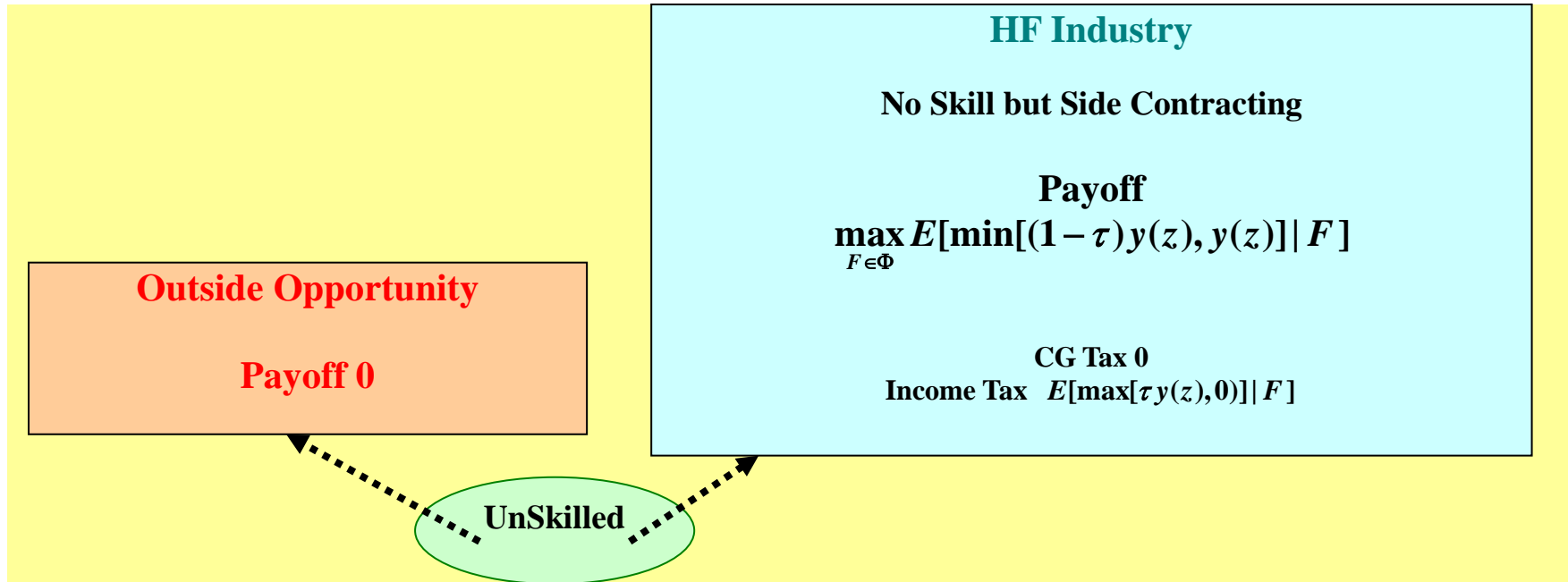
Skilled Entry: $V(y, t, \tau) \geq \bar{V}(t)$



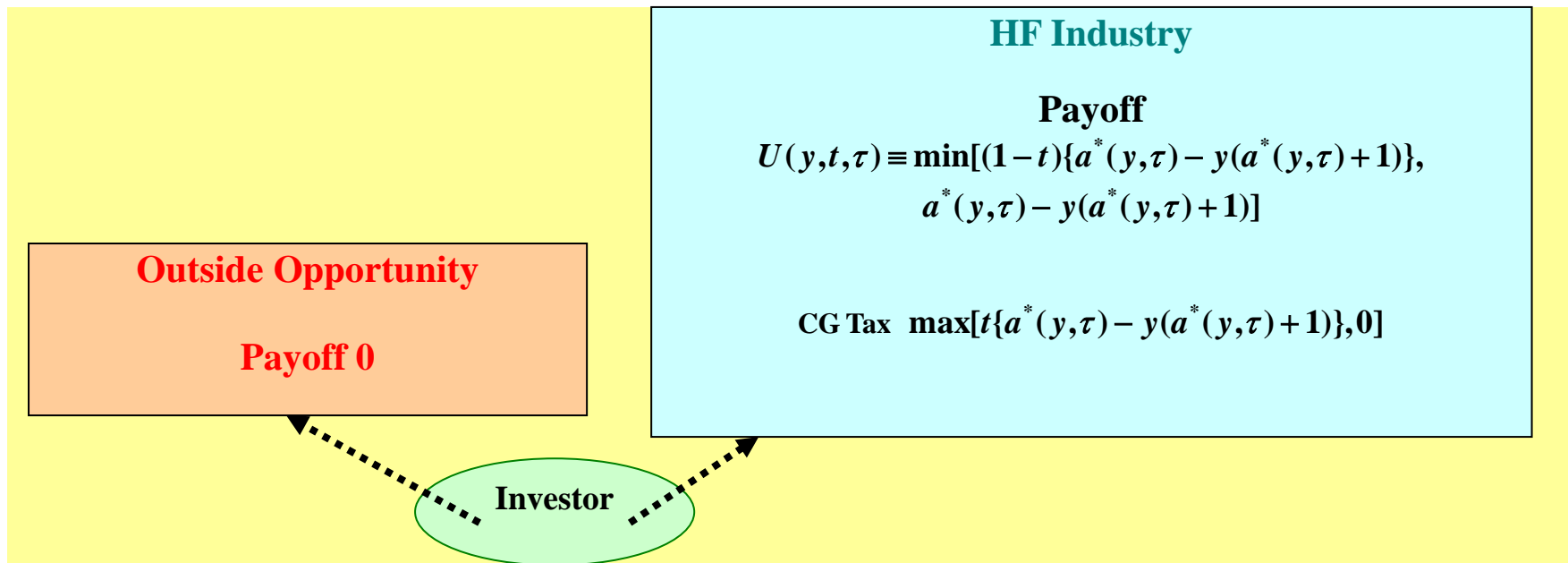
$\tilde{a}(1-t)$ Maximize $(1-t)a - c(a)$

$a^*(y, \tau)$ Maximize $(1-\tau)y(a+1) - c(a)$

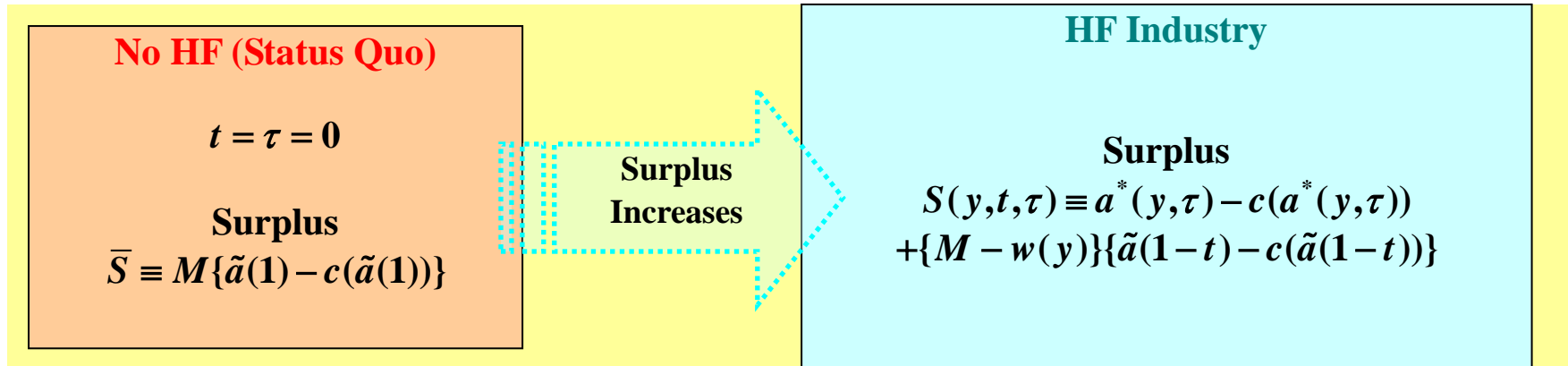
Unskilled Exit: $\max_{F \in \Phi} E[\min[(1 - \tau)y(z), y(z)] | F] \leq 0$



Investor Entry: $U(y,t,\tau) \geq 0$, i.e., $a^*(y,\tau) \geq y(a^*(y,\tau) + 1)$



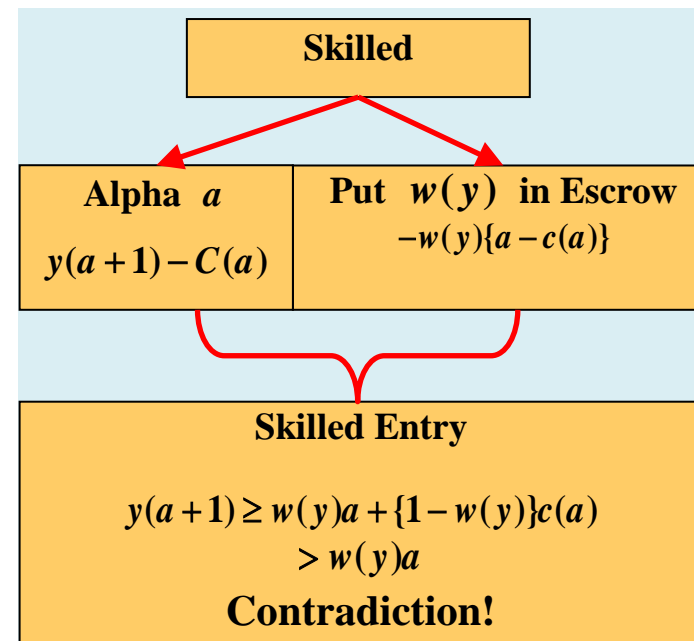
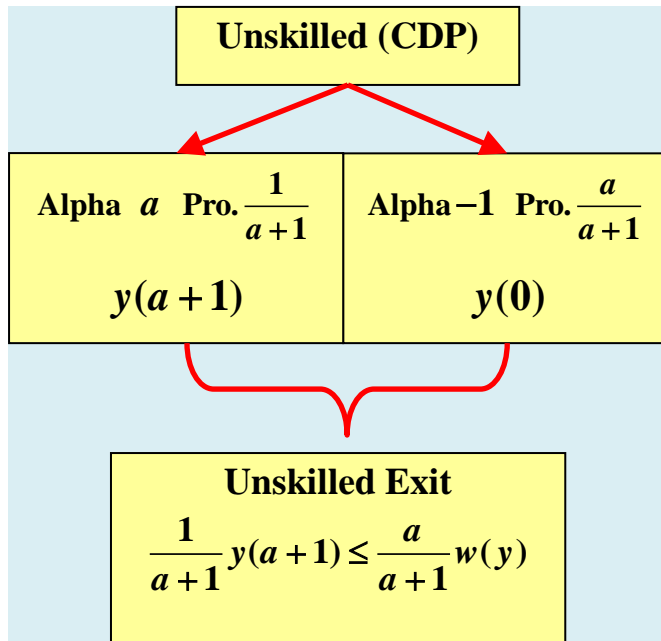
Welfare Improvement: $S(y,t,\tau) > \bar{S}$



No Capital Gain Tax: Impossibility

Theorem: *Suppose CGT Rate $t = 0$. Then, There Exists No Fee Scheme that Satisfies Skilled Entry, Unskilled Exit, and Welfare Improvement.*

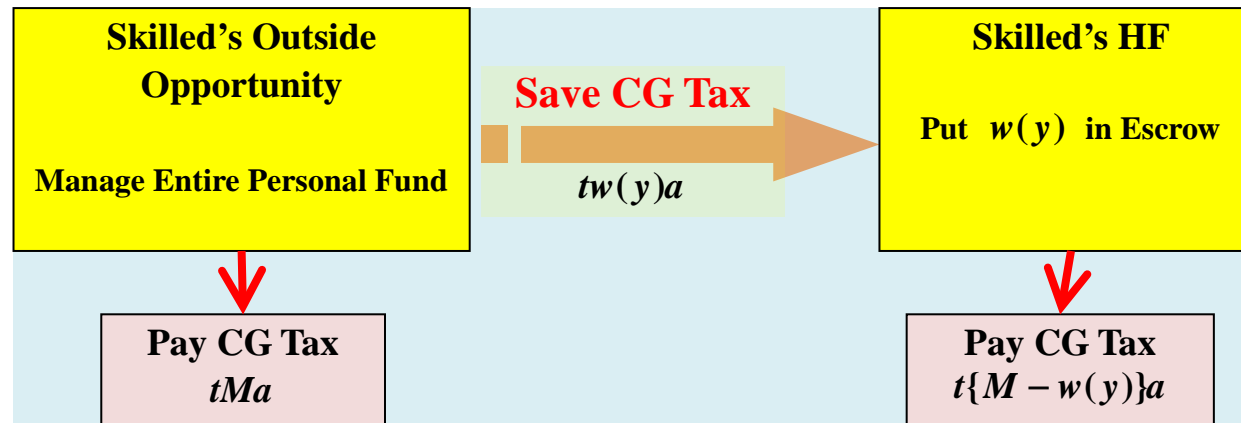
Outline of Proof: Assume $a > 0$ is only available, $y(0) = -w(y)$



Positive Capital Gain Tax: Possibility

Theorem: *There exist Tax Rates $(t, \tau) \in [0, 1]^2$ and Fee Scheme $y \in Y^*(\tau)$ that satisfy All Constraints.*

Outline of Proof: Assume $a > 0$ is only available



“Larger Fund + Less Active” is Better Than “Smaller Fund + More Active”

Constrained Optimization: (y^*, t^*, τ^*)

(1) Fulcrum Scheme after Taxation $y(x) = x - 1$ for all $x \in [1, \infty)$

$y(x) = (1 - \tau)(x - 1)$ for all $x \in [0, 1)$

(2) Skilled Entry Binding

$V(y, t, \tau) = \bar{V}(t)$

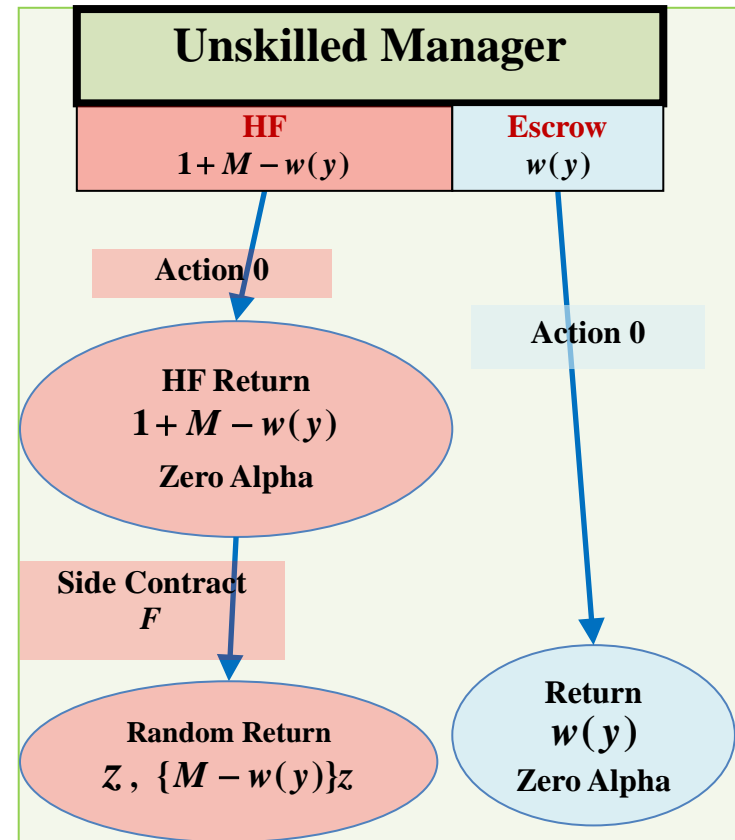
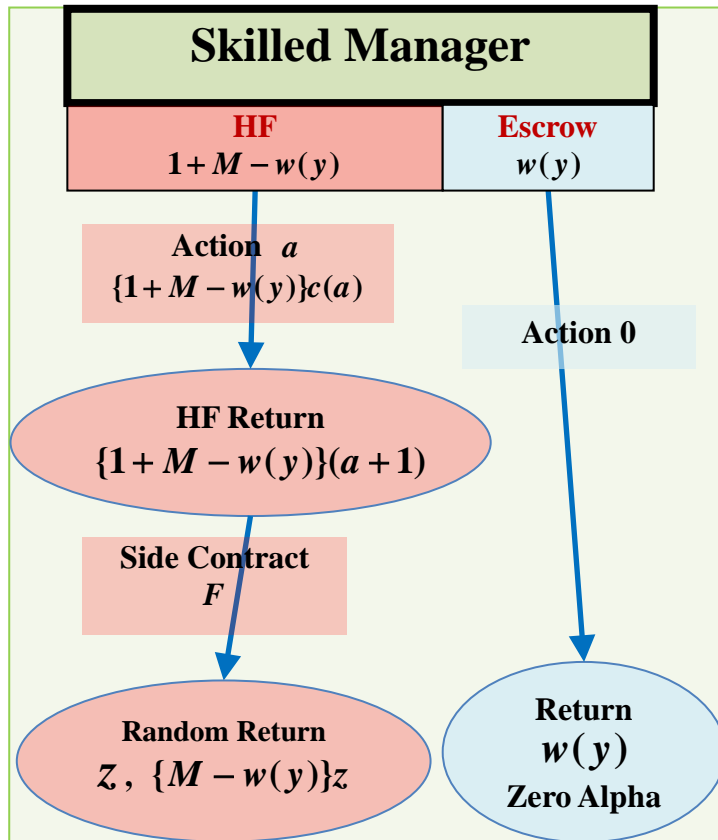
We Specify $(y, t, \tau) = (y^*, t^*, \tau^*)$ As Maximizing Surplus $S(y, t, \tau)$ Subject to **(1)** and **(2)**

Theorem: (y^*, t^*, τ^*) Satisfies All Constraints. There exists No (y, t, τ) that Satisfies All Constraints and $S(y, t, \tau) > S(y^*, t^*, \tau^*)$.

Constrained Optimization: Properties

- **Manager is Willing to Select y^* Voluntarily: y^* is the Only Scheme that Satisfies Skilled Entry, Unskilled Exit, Investor Entry, and Skilled Non-mimicry.**
- **Manager Prefers to Put Personal Fund in Escrow as Large as Possible, Distorting Welfare.**
- **Income Tax Rate τ^* is Greater than CG Tax Rate t^* : High Income Tax Rate**

Another Assumption: Equity Stake



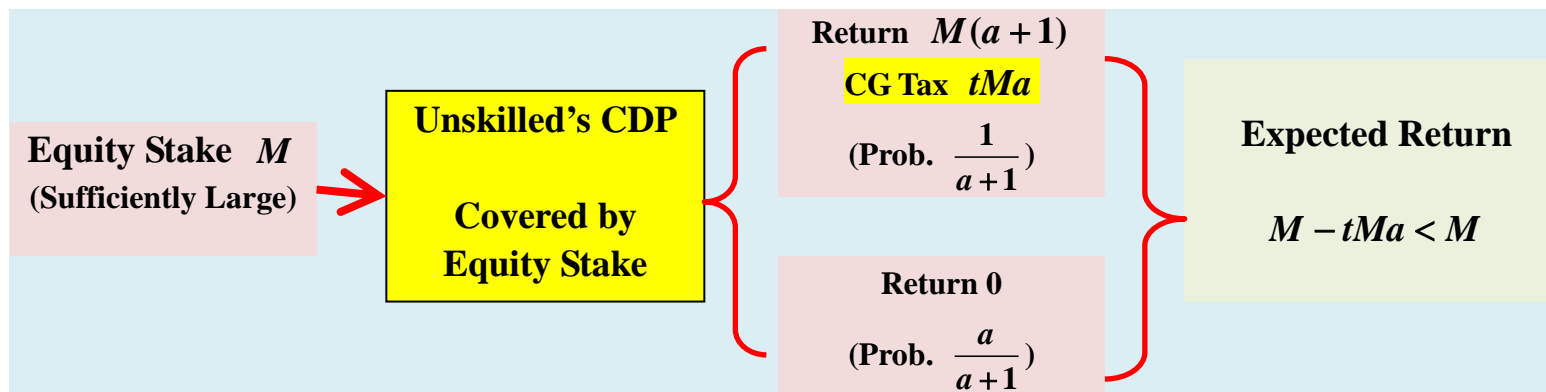
We Don't Need Penalty, But CG Tax and Big Stake

Theorem: *Suppose CGT Rate $t = 0$. Then, There Exists No Fee Scheme that Satisfies Skilled Entry, Unskilled Exit, and Welfare Improvement.*

Additional Assumption: $a > 0$ is only available, $\tau = 0$

Theorem: *For Sufficiently Large Personal Fund M , There exist (t, y) that Levy No Penalty but Satisfy All Constraints.*

Outline of Proof: CDP Must be Covered by Not only Investor's Fund But also Personal Fund



Further Comments

Investor's Optimization

- Investor Prefers **higher**-Powered and **More** Penalty than Constrained Optimal Scheme.
- By Transferring Total Tax Revenue to Investor, Government Can Incentivize Investor to Select Constrained Optimal Scheme Voluntarily.
- Investor's Payoff May be **Greater** than Manager's Payoff per Unit: Manager May Fold HF Business.

Entry Cost

Entry Cost Functions, if, and Only if, It is **Non-Pecuniary!**